Summer 2008

# **INDIANA'S** CORE STANDARDS:

Core Academic Concepts Across the K–12 Continuum A Companion to Indiana's Academic Standards

# MATHEMATICS Kindergarten – Grade 12

KXA

Indiana Department of Education

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Effective curriculum, instruction and assessment do not happen by accident. They are the result of many people planning together, working together and sharing responsibility for the success of all students.

A great deal of work has gone into developing resources to help educators plan curriculum, instruction and assessment. What has made the development process so successful is the grassroots involvement of people statewide. The collaborative efforts and dedication of teachers, administrators, state educational organizations, parents, business leaders, higher education faculty, Indiana Department of Education staff, Board of Education members, Indiana's Education Roundtable and the public have contributed to the creation of quality resources for our teachers.

To continue this work, Indiana has adopted *Core Standards: Core Academic Concepts Across the K-12 Continuum.* The *Core Standards*, a complement to *Indiana's Academic Standards*, explicitly highlight the "big ideas" for each grade level and content area, give proper weight to concepts central to advancement across subsequent grade levels, allow for instructionally-supportive assessments, and encourage the integration of curricula across content areas. The *Core Standards* build upon *Indiana's Academic Standards* by integrating multiple Standard Indicators into a small number of instructionally-coherent targets that reflect priorities for each school year or course.

It is our sincerest hope that the *Core Standards* help teachers' efforts in defining and developing curriculum, selecting instruction, assessing student outcomes and integrating content areas when appropriate to support the success of Indiana's students.

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# 

### **Purpose of the Core Standards**

The Core Standards invite new ways of aligning K-12 curriculum and assessment to Indiana's Academic Standards.

### Core Standards in the Classroom

The teachers can use the Core Standards to:

- help students focus on the key concepts (the most important Standard Indicators necessary for understanding the "big ideas") of each grade level and content area;
- help parents understand the most important concepts to be learned at each grade level;
- inform decision-making when planning and delivering instruction and designing assessment;
- create more focused goals for student performance at the end of each school year; and
- communicate to administrators, school officials and the public that Indiana continues to strive for high standards in education.

### Core Standards in the Education Community

The public can use the Core Standards to:

- gain a clearer understanding of what is expected of Indiana students and teachers;
- enhance discussions of ways to integrate curriculum, instruction and assessment;
- engage in conversations regarding professional development within the K-12 environment;
- explore collaborative opportunities between K-12 teachers and higher education faculty; and
- discuss conceptual learning across and outside the education community.

### THE CORE STANDARDS:

- Highlight the most important concepts presented in each grade level and content area by integrating multiple Standard Indicators from *Indiana's Academic Standards*;
- outline a manageable number of concepts that all students must understand and be able to do at the end of the year;
- emphasize the concepts that are central to each grade and are connected to subsequent grade levels;
- set challenging and explicit goals that delineate which Standard Indicators should receive the most instructional time;
- support the development of assessment that is focused on concepts that are central to a grade level or content area;
- enable teachers to assess critical skills in greater depth and use student responses to guide further instruction; and
- provide the opportunity to integrate multiple content areas in the classroom by analyzing the connections among the manageable lists of concepts in each grade level and content area.

# PROCESS STANDARDS

These Process Standards from the National Council of Teachers of Mathematics address problem-solving skills and are to be used in conjunction with the *Core Standards*.

Indiana's Core Standards – MATHEMATICS

# PROCESS STANDARDS

### To Accompany the Core Standards

Indiana's *Core Standards* for Mathematics describe the key content for students in each grade level and course. Students must develop conceptual understanding of this content. The American Diploma Project noted that, "beyond acquiring procedural mathematical skills with their clear methods and boundaries, students need to master the more subjective skills of reading, interpreting, representing and 'mathematicizing' a problem" (2004, 55). The National Council of Teachers of Mathematics has described five Process Standards that "highlight ways of acquiring and using content knowledge" (2000, 29). The following Process Standards should be addressed throughout the learning and teaching of Indiana's Core Standards for Mathematics in all grade levels.

### **Problem Solving**

- Build new mathematical knowledge through problem solving.
- Solve problems that arise in mathematics and in other contexts.
- Apply and adapt a variety of appropriate strategies to solve problems.
- Monitor and reflect on the process of mathematical problem solving.

### **Reasoning and Proof**

- Recognize reasoning and proof as fundamental aspects of mathematics.
- Make and investigate mathematical conjectures.
- Develop and evaluate mathematical arguments and proofs.
- Select and use various types of reasoning and methods of proof.

### Communication

- Organize and consolidate mathematical thinking through communication.
- Communicate mathematical thinking coherently and clearly to peers, teachers and others.
- Analyze and evaluate the mathematical thinking and strategies of others.
- Use the language of mathematics to express mathematical ideas precisely.

# PROCESS STANDARDS

### Connections

- Recognize and use connections among mathematical ideas.
- Understand how mathematical ideas interconnect and build on one another to produce a coherent whole.
- Recognize and apply mathematics in contexts outside of mathematics.

### Representation

- Create and use representations to organize, record and communicate mathematical ideas.
- Select, apply and translate among mathematical representations to solve problems.
- Use representations to model and interpret physical, social and mathematical phenomena.

### Technology

Technology should be used as an essential tool in mathematics education to support and extend the mathematics curriculum. Technology can contribute to concept development, simulation, representation, communication and problem solving. The challenge is to ensure that technology supports-but is not a substitute for-the development of skills with basic operations, quantitative reasoning and problem-solving skills. Elementary students must learn how to perform thoroughly the basic arithmetic operations independent of the use of a calculator. Graphing calculators must be used to enhance middle school and high school students' understanding and skills rather than replace them. The focus must be on learning mathematics, using technology as a tool rather than as an end in itself.

### References

American Diploma Project. 2004. Ready or Not: Creating a High School Diploma that Counts. Washington, DC: Achieve, Inc.

National Council of Teachers of Mathematics. 2000. Principles and Standards for School Mathematics. Reston, VA: NCTM.

# CORE STANDARDS

The *Core Standards* represent ideas that are broad in scope and encompass multiple Standard Indicators. Students should be proficient in these *Core Standards* in order to successfully move on to the next levels of Mathematics.

Indiana's Core Standards – MATHEMATICS

### **Core Standards for Kindergarten Mathematics**

#### CORE STANDARD

### Number Sense and Computation

1

### Counting to 20

Count objects and use symbols (numerals and pictures) and names to represent whole numbers up to 20. Find the number that is one more than or one less than any whole number up to 20. Recognize numbers from 10 to 20 and represent them as groups of tens and ones. Show equivalent forms of the same number (up to 20) using objects, diagrams and numerals.

[Standard Indicators: K.1.6, K.1.7]

### CORE STANDARD 2

### Geometry and Measurement

### Comparing and Classifying Objects

Identify, describe, sort, compare and classify objects by shape, size, number of vertices and other attributes.

[Standard Indicators: K.3.1, K.4.1, K.4.2]

### **Comparing Measures**

Make direct comparisons of the length, capacity, weight and temperature of objects and recognize which object is shorter, longer, taller, lighter, heavier, warmer, cooler or holds more.

[Standard Indicator: K.5.1]



### Core Standards for Grade 1 Mathematics

#### CORE STANDARD

### Number Sense and Computation

1

### Whole Numbers

Count, read, write and compare whole numbers up to 100. Recognize numbers up to 100 and represent them as groups of tens and ones.

[Standard Indicators: 1.1.1, 1.1.2, 1.1.3, 1.1.4, 1.1.5]

### Addition and Subtraction

Model addition and subtraction using objects. Demonstrate fluency with addition facts (for totals up to 20) and the corresponding subtraction facts. Solve problems involving addition and subtraction.

[Standard Indicators: 1.2.1, 1.2.2, 1.2.4, 1.2.5, 1.2.6, 1.2.7, 1.3.1]

### CORE STANDARD 2

### Geometry and Measurement

### Geometric Shapes

Identify, describe, compare, sort and draw triangles, rectangles, squares and circles.

[Standard Indicators: 1.4.1, 1.4.2, 1.4.7]

### Linear Measurement

Estimate and measure the length of an object to the nearest inch and centimeter.

[Standard Indicator: 1.5.4]



### **Core Standards for Grade 2 Mathematics**

#### CORE STANDARD

### Number Sense and Computation

1

### Place Value

Understand and use the relationship among whole numbers, including place value, to identify and compare numbers up to 1000.

[Standard Indicators: 2.1.1, 2.1.2, 2.1.3, 2.1.4, 2.1.5, 2.1.7]

### Addition and Subtraction

Add and subtract whole numbers less than 1000 using efficient methods. Understand and show the inverse relationship between addition and subtraction.

[Standard Indicators: 2.2.1, 2.2.2, 2.2.3, 2.2.4, 2.2.6, 2.3.1, 2.3.4]

### CORE STANDARD 2

### **Geometry and Measurement**

### Common Shapes and Objects

Recognize, identify, and describe attributes of common shapes and solids (e.g., the same size and type of shape; number of sides, edges, vertices; location).

[Standard Indicators: 2.4.2, 2.4.4, 2.4.5]

### Linear Measurement

Understand and use units of linear measurement and relationships within a particular system to solve problems. Measure lengths in standard units (e.g., inches, feet and yards) and metric units (e.g., centimeters and meters) and select appropriate units to estimate and measure lengths.

[Standard Indicators: 2.5.1, 2.5.2, 2.5.3]



### **Core Standards for Grade 3 Mathematics**

#### CORE STANDARD

### Number Sense and Computation

1

### Place Value

Understand and use the relationship among whole numbers, including place value, to identify and compare numbers up to 10,000.

[Standard Indicators: 3.1.1, 3.1.2, 3.1.3, 3.1.4, 3.1.5, 3.1.7, 3.3.7]

### Interpreting and Modeling Fractions

Interpret and model fractions as parts of a whole, parts of a group, and points and distances on a number line. Solve problems that involve comparing and ordering fractions.

[Standard Indicators: 3.1.8, 3.1.10]

### Addition and Subtraction

Understand and use standard algorithms for addition and subtraction.

[Standard Indicators: 3.2.1, 3.2.8, 3.3.1, 3.3.2]

### Multiplication and Division

Understand the meaning of multiplication and division of whole numbers and show the relationship between them. Find values for number sentences containing multiplication and/or division.

[Standard Indicators: 3.2.2, 3.2.3, 3.2.4, 3.2.5, 3.3.1, 3.3.2, 3.3.4, 3.3.5]

### CORE STANDARD 2

#### **Geometry and Measurement**

#### Points and Lines

Identify, describe and draw points, lines and line segments.

[Standard Indicators: 3.4.6, 3.4.7]

### Length, Weight and Unit Conversions

Choose and use appropriate units and tools to estimate and measure length and weight. Carry out simple unit conversions within a measurement system.

[Standard Indicators: 3.5.1, 3.5.2, 3.5.6, 3.5.7, 3.5.8, 3.5.9, 3.5.11, 3.5.12]



### **Core Standards for Grade 4 Mathematics**

#### CORE STANDARD

### Number Sense and Computation

### Place Value

Understand and use the relationship among whole numbers, including place value, to identify and compare numbers. Interpret and model decimals as parts of a whole, parts of a group, and points and distances on a number line.

[Standard Indicators: 4.1.1, 4.1.2, 4.1.4, 4.1.8, 4.1.9]

### Multiplication and Division Facts

Demonstrate fluency with multiplication facts for numbers up to 10 and related division facts.

[Standard Indicator: 4.2.4]

### Multiplying Whole Numbers

Multiply numbers up to 100 by single-digit numbers and by 10, solving problems written horizontally and vertically.

[Standard Indicators: 4.2.1, 4.2.5, 4.2.6, 4.2.7, 4.2.12, 4.3.5, 4.3.7]

### Addition and Subtraction of Fractions

Model addition and subtraction of simple fractions.

[Standard Indicator: 4.2.8]

### CORE STANDARD 2

### Geometry and Measurement

### Angles and Lines

Identify, describe and draw parallel and perpendicular lines, and right, acute, obtuse and straight angles.

[Standard Indicators: 4.4.1, 4.4.2]

### Rectangles

Find and use the perimeter and area of rectangles, including squares.

[Standard Indicators: 4.5.3, 4.5.4]



### **Core Standards for Grade 5 Mathematics**

### CORE STANDARD

### Number Sense and Computation

### Multiplication and Division of Whole Numbers

Multiply and divide whole numbers. Understand and use standard algorithms for multiplication and division.

[Standard Indicator: 5.2.1]

### Comparing Fractions, Decimals and Percents

Compare fractions, decimals and common percents.

[Standard Indicators: 5.1.3, 5.1.4, 5.1.7]

### Addition and Subtraction of Fractions and Decimals

Understand and perform addition and subtraction with fractions, including fractions with different denominators and mixed numbers. Add and subtract decimals, including money in decimal notation.

[Standard Indicators: 5.2.2, 5.2.5, 5.2.7, 5.5.7]

### CORE STANDARD 2

### Geometry and Measurement

### Polygons

Measure angles and describe angles in degrees, and identify, classify and draw polygons and triangles.

[Standard Indicators: 5.4.1, 5.4.2, 5.4.3, 5.4.4]

### Shapes and Solids

Find and use the perimeter and area of triangles, parallelograms and trapezoids, and the surface area and volume of rectangular prisms.

[Standard Indicators: 5.5.1, 5.5.2, 5.5.3, 5.5.4]

CORE 3

### **Algebra and Functions**

### Variables

Evaluate simple algebraic expressions.

[Standard Indicators: 5.3.1, 5.3.2]

### Coordinate Grids

Use two-dimensional coordinate grids to represent points in the first quadrant that fit linear equations. Draw the line determined by the points.

[Standard Indicators: 5.3.4, 5.3.5]



### Core Standards for Grade 6 Mathematics

### CORE STANDARD

### Number Sense and Computation

### Positive and Negative Numbers

Understand and apply the concept of positive and negative numbers. Add, subtract, multiply and divide positive and negative integers. Represent negative numbers, and computation with negative numbers, on a number line.

[Standard Indicators: 6.1.1, 6.1.3, 6.2.1, 6.2.2]

### Percent Representations

Use percents to represent parts of a whole. Represent numbers as fractions, decimals and percents.

[Standard Indicators: 6.1.4, 6.1.5]

### *Multiplication and Division of Fractions and Decimals*

Understand and perform multiplication and division with positive decimals and fractions.

[Standard Indicators: 6.2.3, 6.2.4, 6.2.5, 6.5.10]

### Ratio and Rate

Solve simple ratio and rate problems using multiplication and division.

[Standard Indicators: 6.1.6, 6.2.6, 6.2.7, 6.2.8]

### CORE STANDARD 2

### Geometry and Measurement

### Angles and Polygons

Use properties of complementary, supplementary and vertical angles, and properties of triangles and quadrilaterals to find missing angles.

[Standard Indicators: 6.4.1, 6.4.2, 6.4.4]

### Shapes and Solids

Find and use the circumference and area of circles and the surface area of right prisms and cylinders.

[Standard Indicators: 6.5.4, 6.5.8]



### Core Standards for Grade 6 Mathematics (cont.)

CORE 3

### **Algebra and Functions**

Linear Equations

Write and solve one-step equations and inequalities in one variable.

[Standard Indicators: 6.3.1, 6.3.3, 6.3.6]

### Linear Functions

Write equations of linear functions representing a given situation and graph the resulting ordered pairs of integers on a coordinate grid.

[Standard Indicators: 6.3.7, 6.3.8]



### Core Standards for Grade 7 Mathematics

#### CORE STANDARD

### Number Sense and Computation

1

### Exponents

Use whole number exponents for repeated multiplication. Use scientific notation for large numbers.

[Standard Indicators: 7.1.1, 7.1.4, 7.1.5]

### Proportions and Percentages

Use proportions and percentages to solve application problems involving the increase of a quantity and the decrease of a quantity. Solve problems involving percent, ratio, rate and similar triangles.

[Standard Indicators: 7.2.2, 7.2.3, 7.5.2, 7.5.3]

### Multiplication and Division With Fractions and Decimals

Understand and perform multiplication and division with negative decimals and fractions.

[Standard Indicator: 7.2.1]

### CORE STANDARD 2

### Geometry and Measurement

### Transformations

Identify and use the following transformations: translations, rotations and reflections.

[Standard Indicator: 7.4.2]

### Solids

Find and use the surface area and volume of prisms and cylinders.

[Standard Indicators: 7.5.4, 7.5.5, 7.5.6]



### Core Standards for Grade 7 Mathematics (cont.)

#### CORE STANDARD

### **Algebra and Functions**

#### Expressions

Evaluate numerical expressions and simplify algebraic expressions involving rational and irrational numbers.

3

[Standard Indicators: 7.2.1, 7.3.1, 7.3.4]

### Linear Equations

Write and solve two-step equations and inequalities in one variable.

[Standard Indicators: 7.3.1, 7.3.2]

### Graphs of Lines

Find the slope of a line from its graph. Relate the slope of a line to similar triangles. Draw the graph of a line given its slope. Graph proportional relationships and identify the unit rate as the slope of the related line.

[Standard Indicators: 7.3.6, 7.3.7, 7.3.8, 7.3.9, 7.3.10]

### CORE STANDARD 4

#### Data Analysis and Probability

### Making Estimates and Data Displays

Use proportions to make estimates about a population based on a sample. Create, analyze and interpret data sets in multiple ways using bar graphs, frequency tables, line plots, histograms and circle graphs.

[Standard Indicators: 7.6.1, 7.6.2]

#### Theoretical Probability

Understand that when all outcomes of an experiment are equally likely, the theoretical probability of an event is the fraction of outcomes in which the event occurs. Use theoretical probability and proportions to make predictions.

[Standard Indicators: Forthcoming]



### **Core Standards for Grade 8 Mathematics**

### CORE STANDARD

### Number Sense and Computation

### Integer Exponents

Use the laws of integer exponents and evaluate expressions with negative integer exponents. Use scientific notation for small numbers.

[Standard Indicators: 8.1.1, 8.1.4, 8.1.5]

### Square Roots

Use irrational numbers. Calculate square roots. Use the inverse relationship between squares and square roots.

[Standard Indicators: 8.1.2, 8.1.6, 8.1.7]

### CORE STANDARD 2

#### Geometry and Measurement

### Constructions and Properties of Shapes

Perform basic compass and straightedge constructions, such as constructions of angle and segment bisectors, copies of segments and angles, and perpendicular segments. Justify the constructions. Identify properties of geometric shapes.

[Standard Indicators: 8.4.1, 8.4.2]

### Pythagorean Theorem

Use the Pythagorean Theorem and its converse to calculate lengths of line segments such as the altitude of an equilateral triangle, the diagonal of a rectangular prism, or the chord of a circle that subtends a right angle.

[Standard Indicator: 8.4.5]

#### Rates

Solve simple problems involving rates and derived measurements such as speed and density. Express measurements in a given unit in terms of other units of the same types, such as *miles per hour* in terms of *feet per second*.

[Standard Indicators: 8.5.1, 8.5.2]



### Core Standards for Grade 8 Mathematics (cont.)

CORE STANDARD

2 cont.

### Geometry and Measurement

### Solids

Find and use the surface areas and volumes of cones, spheres and pyramids. Use scale factors to find areas and volumes of similar figures.

[Standard Indicators: 8.5.3, 8.5.4, 8.5.5]

3

CORE STANDARD

#### **Algebra and Functions**

#### Solving Equations and Inequalities

Write and solve multi-step equations and inequalities in one variable.

[Standard Indicators: 8.2.1, 8.3.1, 8.3.4]

#### Linear Functions

Use linear functions and linear equations to represent, analyze and solve problems. Translate among tables, equations, verbal expressions and graphs.

[Standard Indicators: 8.3.5, 8.3.6, 8.3.8]

### CORE STANDARD 4

### Data Analysis and Probability

#### Analyzing Data

Use mean, median, mode, upper and lower quartiles, and range of data to compare data sets. Organize and display data to analyze central tendencies of data. Investigate effects of change in data values on the measures of the central tendency of the set of data. Display data in scatter plots, informally finding lines of best fit.

### [Standard Indicators: 8.6.3, 8.6.4, 8.6.5]

### *Evaluating Claims, Selecting Samples and Analyzing Bias*

Identify claims based on statistical data and, in simple cases, evaluate the reasonableness of the claims. Identify different methods of selecting samples, analyzing the strengths and weaknesses of each method, and the possible bias in a sample or display.

[Standard Indicators: 8.6.1, 8.6.2]

#### Simple Experiments

Compute probabilities of events from simple experiments with equally probable outcomes.

[Standard Indicator: 8.6.6]



### Core Standards for Algebra I

#### CORE STANDARD

### **Rational Exponents**

Understand and use the laws of exponents for variables with exponents. Multiply, divide, and find powers of variables with exponents.

### [Standard Indicators: A1.1.4, A1.6.3]



### d 2

### **Relations and Functions**

Determine whether a relation is a function or not a function. Identify the domain and range of a given relation. Sketch and interpret linear and non-linear graphs representing given situations. Translate among verbal descriptions, tables, graphs and equations.

[Standard Indicators: A1.3.1, A1.3.2, A1.3.3, A1.3.4]

CORE	2
STANDARD	0

### Linear Equations, Functions and Inequalities

### Graphing and Writing Linear Equations

Graph linear functions and determine their slopes and *x*- and *y*- intercepts from their graphs and equations. Write a linear function in slope-intercept form. Determine the equation of a line given sufficient information.

[Standard Indicators: A1.4.1, A1.4.2, A1.4.3, A1.4.4, A1.4.5]



### Linear Equations, Functions and Inequalities

### Pairs of Linear Equations in Two Variables

Solve pairs of linear equations in two variables by graphing, substitution or elimination. Solve problems that can be modeled using pairs of linear equations in two variables.

[Standard Indicators: A1.5.1, A1.5.3, A1.5.4, A1.5.5, A1.5.6]



### Core Standards for Algebra I (cont.)

CORE STANDARD

### Linear Equations, Functions and Inequalities

### Pairs of Linear Inequalities in Two Variables

5

Graph the solution for pairs of linear inequalities in two variables.

[Standard Indicator: A1.5.2]

CORE STANDARD

### **Polynomials**

Multiply polynomials, factor polynomials, and divide a polynomial by a monomial.

6

[Standard Indicators: A1.6.2, A1.6.4, A1.6.5, A1.6.6, A1.6.7]

CORE	7
STANDARD	

#### **Quadratic Equations and Functions**

Solve quadratic equations by graphing, factoring, and using the quadratic formula. Graph quadratic functions and understand the relationship between its zeros and the *x*-intercepts of its graph.

[Standard Indicators: A1.6.8, A1.8.1, A1.8.2, A1.8.3, A1.8.4, A1.8.6, A1.8.7]

## 

### Core Standards for Geometry

2

#### CORE STANDARD

### **Angles and Lines**

Understand the relationship between special angles created by parallel lines and transversals.

### [Standard Indicator: G.1.3]

CORE STANDARD

**Congruence and Similarity** 

Use theorems to show whether two triangles are congruent or similar and to find more information about pairs of congruent triangles. Solve problems involving congruent and similar polygons and solids.

[Standard Indicators: G.2.3, G.3.2, G.4.4, G.4.6, G.5.6, G.7.6]

3

CORE STANDARD

#### Triangles

Prove the Pythagorean Theorem and its converse and use them to solve problems involving the length of a segment in the coordinate plane. For general triangles, prove that the sum of the angles is 180 degrees. Define trigonometric functions in terms of angles of right triangles and use them to solve problems.

[Standard Indicators: G.5.1, G.5.3, G.5.4, G.5.6]

### CORE STANDARD 4

### Polygons

Find the sum of the measures of the interior and exterior angles of convex polygons. Deduce formulas relating lengths and sides, perimeters, and areas of regular polygons, and understand how limiting cases of such formulas lead to expressions for the circumference and the area of a circle.

### [Standard Indicators: G.2.2, G.2.5, G.6.7]

### Circles

Define, deduce and use formulas for, and prove theorems for:

- radius, diameter, arc, chord, secant and tangent;
- measures of arcs and related angles (central, inscribed, and intersections of secants and tangents); and
- circumference, arc length and areas of circles and sectors.

Determine how the graph of a circle changes if a, b, and r are changed in the equation  $(x - a)^2 + (y - b)^2 = r^2$ .

[Standard Indicators: G.6.2, G.6.5, G.6.7, G.6.8]



### Core Standards for Geometry (cont.)

CORE **6** 

#### Solids

Find and use measures of sides, volumes of solids, and surface areas of solids. Relate these measures to each other using formulas.

[Standard Indicator: G.7.7]

CORE STANDARD

#### **Coordinate Geometry**

Find slopes, lengths and midpoints of line segments using coordinate geometry. Use these measures to show whether shapes are similar or congruent, and whether line segments are parallel or perpendicular. Find the equation of a circle in the coordinate plane.

[Standard Indicators: G.1.1, G.1.4, G.2.6, G.3.4, G.4.9, G.6.8]

### CORE STANDARD 8

#### Transformations

Predict and describe the results of translations, reflections and rotations. Describe a motion or series of motions that will show that two shapes are congruent.

#### [Standard Indicator: G.2.4]



### Geometric Proof and Reasoning

Understand the difference between supporting evidence, counterexamples and actual proofs. Be able to develop simple geometric proofs involving the following and provide reasons for each statement:

- parallel lines and transversals;
- congruent and similar polygons, particularly triangles;
- circles; and
- geometric objects in the coordinate plane.

[Standard Indicators: G.2.6, G.3.4, G.4.9, G.6.3, G.8.3, G.8.7, G.8.8]

# 

### Core Standards for Algebra II

#### CORE STANDARD

### Linear and Absolute Value Equations and Inequalities

Solve equations and inequalities involving absolute value. Solve systems of linear equations and inequalities in three variables by substitution and elimination. Solve problems that can be modeled using systems of linear equations.

[Standard Indicators: A2.2.1, A2.2.2, A2.2.3]



### **Complex Numbers**

Add, subtract, multiply and divide complex numbers.

[Standard Indicator: A2.3.1]



### **Quadratic Equations and Functions**

3

### Solving Quadratic Equations

Solve quadratic equations in the complex number system. Solve problems that can be modeled using quadratic equations and functions.

[Standard Indicators: A2.3.3, A2.3.5]

CORE	6
STANDARD	4

### **Quadratic Equations and Functions**

### Graphing Quadratic Functions

Graph quadratic functions. Determine how the graph of a parabola changes if *a*, *b*, and *c* are changed in the equation  $y = a(x - b)^2 + c$ . Find an equation for a parabola given sufficient information.

[Standard Indicator: A2.3.4]



### **Polynomial Equations and Functions**

#### Solving Polynomial Equations

Solve polynomial equations by factoring. Solve problems that can be modeled using polynomial equations.

[Standard Indicators: A2.5.3, A2.5.5]

# ALGEBRA III

### Core Standards for Algebra II (cont.)

CORE STANDARD

### **Polynomial Equations and Functions**

6

### Writing Polynomial Equations

Perform arithmetic operations, including long division, on polynomials. Find a polynomial given its roots and use the relationship between solutions of an equation, zeros of a function, *x*-intercepts of a graph and factors of a polynomial expression to solve problems.

[Standard Indicators: A2.5.2, A2.5.6, A2.5.7]

CORE STANDARD

### **Polynomial Equations and Functions**

### Rational Functions

Add, subtract, multiply, divide, reduce and evaluate rational expressions with polynomial denominators. Simplify rational expressions including expressions with negative exponents in the denominator. Solve problems that can be modeled using equations involving rational functions.

[Standard Indicators: A2.6.1, A2.6.2, A2.6.3, A2.6.4, A2.6.5]

CORE	0
STANDARD	0

### **Exponential and Logarithmic Equations**

Use laws of exponents to derive laws of logarithms. Use laws of logarithms to solve problems. Solve exponential and logarithmic equations. Solve problems that can be modeled using equations involving exponents and logarithms.

[Standard Indicators: A2.7.2, A2.7.3, A2.7.4, A2.7.8]

#### Sequences and Series

Find specific terms of arithmetic and geometric sequences. Find partial sums of arithmetic and geometric series. Solve problems that can be modeled using arithmetic and geometric series.

[Standard Indicators: A2.8.2, A2.8.3, A2.8.4]

CORE	10
STANDARD	10

#### **Combinatorics and Probability**

Use permutations, combinations and other counting methods to determine the number of ways that events can occur. Calculate the probability of compound events, and analyze probabilities to interpret odds and risks of events.

[Standard Indicators: A2.9.1, A2.9.2]

## PRE-CALCULUS

### **Core Standards for Pre-Calculus**

#### CORE STANDARD

### **Graphing Functions**

Use paper and pencil methods and graphing technology to graph polynomial, absolute value, rational, algebraic, exponential, logarithmic, trigonometric and inverse trigonometric functions. Identify domain, range, intercepts, zeros, asymptotes and points of discontinuity of functions. Use graphs to solve problems.

[Standard Indicators: PC.1.1, PC.1.2, PC.1.3, PC.2.1, PC.2.2, PC.2.3, PC.4.5, PC.4.6, PC.4.8]

core 2
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### **Conic Sections**

Derive equations for conic sections. Graph conic sections by hand by completing the square and find foci, centers, asymptotes, eccentricity, axes and vertices (as appropriate).

[Standard Indicator: PC.1.10]

CORE	2
STANDARD	5

### Logarithmic and Exponential Functions

Define and find inverse functions. Verify whether two given functions are inverses of each other. Solve problems involving logarithmic and exponential functions using the laws of logarithms and understand why those properties are true.

### [Standard Indicators: PC.1.4, PC.2.1, PC.2.4]



### Unit Circle

Define sine and cosine using the unit circle, converting between degree and radian measures. Use the values of the sine, cosine and tangent functions at 0,  $\pi$ /6,  $\pi$ /4,  $\pi$ /3 and  $\pi$ /2 radians and their multiples.

[Standard Indicators: PC.4.1, PC.4.2, PC.4.3]

#### CORE STANDARD

#### **Trigonometric Functions**

Define and analyze trigonometric functions, including inverse functions. Solve problems involving trigonometric functions and prove trigonometric identities.

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[Standard Indicators: PC.4.4, PC.4.5, PC.4.6, PC.4.8, PC.4.9, PC.5.1, PC.5.2, PC.5.3, PC.5.4, PC.5.5, PC.5.6]

# PRE-CALCULUS

### Core Standards for Pre-Calculus (cont.)

#### CORE STANDARD

### Polar Coordinates and Complex Numbers

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Define and use polar coordinates and complex numbers. Graph equations in the polar coordinate plane. Use their relation to trigonometric functions to solve problems.

[Standard Indicators: PC.6.1, PC.6.2, PC.6.3, PC.6.4]



#### **Sequences and Series**

Define arithmetic and geometric sequences and series. Prove and use the sum formulas for arithmetic series and for finite and infinite geometric series. Understand and use the concept of a limit of a sequence or function as the independent variable approaches infinity or a number, and recognize an infinite series as the limit of a sequence of partial sums. Use series to solve problems. Derive the binomial theorem by combinatorics.

[Standard Indicators: PC.7.1, PC.7.2, PC.7.3]